CURRICULUM VITAE

Personal Information:

Name: Sabyasachi Mukherjee

Date of Birth: 4th February, 1986

Nationality: Indian

Official Address: School of Mathematics, Tata Institute of Fundamental Research, 1 Homi Bhabha

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Employment:

• Current position: Reader at Tata Institute of Fundamental Research, India since July 2019.

• Previous position: Lecturer in Institute for Mathematical Sciences, Stony Brook University, USA (2015-2019).

Academic Information:

- 1. 2007: Bachelor of Science (Mathematics, Physics, and Computer Science) from University of Calcutta, India.
- 2. 2009: Master of Science (Pure Mathematics) from University of Calcutta, India.
- 3. 2011 : 'Master mention Mathématiques et Informatique' (Masters in Mathematics and Informatics) from Université Paris 13, France.
- 4. 2015: Ph.D. in Mathematics from Jacobs University Bremen, Germany.

Ph.D. thesis:

Title:

Antiholomorphic dynamics: topology of parameter spaces, and discontinuity of straightening.

Ph.D. adviser:

Dierk Schleicher, Jacobs University, Bremen, Germany.

Jury:

John Hamal Hubbard (Cornell University), Alan Huckleberry (Ruhr-Universität Bochum/Jacobs University), Hiroyuki Inou (Kyoto University), Keivan Mallahi-Karai (Jacobs University), John Milnor (Stony Brook University), Dierk Schleicher (Jacobs University).

M.Sc. dissertation:

Title:

A detailed proof of Melnikov's theorem on persistence of lower-dimensional tori in nearly integrable Hamiltonian systems, and deduction of the classical KAM theorem.

Adviser of M.Sc. dissertation:

Ricardo Perez-Marco, Université Paris 13, Paris, France.

Research Interest:

Conformal dynamics, complex analysis.

Papers/Pre-prints:

1. Orbit portraits of unicritical antiholomorphic polynomials, Conformal Geometry and Dynamics of the AMS, 19:35–50, 2015.

http://www.ams.org/journals/ecgd/2015-19-03/S1088-4173-2015-00276-3/.

2. Non-landing parameter rays of the Multicorns (joint work with Hiroyuki Inou), *Inventiones Mathematicae*, 204(3):869–893, 2016.

http://link.springer.com/article/10.1007/s00222-015-0627-3.

3. Rational parameter rays of Multibrot sets (joint work with Dierk Schleicher and Dominik Eberlein), *Dynamical Systems, Number Theory and Applications*, chapter 3, pages 49–84, World Scientific, 2016.

http://dx.doi.org/10.1142/9789814699877_0003.

4. On Multicorns and Unicorns II: bifurcations in spaces of antiholomorphic polynomials (joint work with Dierk Schleicher and Shizuo Nakane), *Ergodic Theory and Dynamical Systems*, 37:859–899, 2017.

http://journals.cambridge.org/abstract_S0143385715000656.

- 5. Parabolic arcs of the Multicorns: real-analyticity of Hausdorff dimension, and singularities of Per_n(1) curves, *Discrete and Continuous Dynamical Systems-A*, 37:2565–2588, 2017. http://www.aimsciences.org/article/doi/10.3934/dcds.2017110.
- Antiholomorphic perturbations of Weierstrass Zeta functions and Green's function on tori (joint work with Konstantin Bogdanov, Khudoyor Mamayusupov, and Dierk Schleicher), Nonlinearity, 30:3241–3254, 2017.

https://doi.org/10.1088/1361-6544/aa79cf.

- 7. A rigidity result for some parabolic germs (joint work with Luna Lomonaco), *Indiana University Mathematics Journal*, 67:2089-2101, 2018. http://www.iumj.indiana.edu/oai/2018/67/7459/7459.xml.
- 8. On the support of the bifurcation measure of cubic polynomials (joint work with Hiroyuki Inou), *Mathematische Annalen*, 378:1-12, 2020.
 - $\verb|https://link.springer.com/article/10.1007/s00208-019-01826-3|.$
- 9. Invisible Tricorns in real slices of rational maps (joint work with Russell Lodge), Discrete and Continuous Dynamical Systems-A, 41:1755-1797, 2021.

https://www.aimsciences.org/article/doi/10.3934/dcds.2020340.

- 10. Discontinuity of straightening in anti-holomorphic dynamics: I (joint work with Hiroyuki Inou), Transactions of the American Mathematical Society, 374:6445-6481, 2021. https://doi.org/10.1090/tran/8381.
- 11. Schwarz reflections and anti-holomorphic correspondences (joint work with Seung-Yeop Lee, Mikhail Lyubich, and Nikolai Makarov), *Advances in Mathematics*, 385:107766, 2021. https://doi.org/10.1016/j.aim.2021.107766.
- 12. Univalent polynomials and Hubbard trees (joint work with Kirill Lazebnik and Nikolai Makarov), *Transactions of the American Mathematical Society*, 374:4839-4893, 2021. https://doi.org/10.1090/tran/8387.
- 13. Bers slices in families of univalent maps (joint work with Kirill Lazebnik and Nikolai Makarov), Mathematische Zeitschrift, 300:2771-2808, 2022. https://doi.org/10.1007/s00209-021-02871-y.
- 14. Circle packings, kissing reflection groups, and critically fixed anti-rational maps (joint work with Russell Lodge and Yusheng Luo), Forum of Mathematics, Sigma, vol. 10, e3, 2022. https://doi.org/10.1017/fms.2021.81.
- 15. Discontinuity of straightening in anti-holomorphic dynamics: II (joint work with Hiroyuki Inou), *International Mathematics Research Notices*, 2022(9):6948–6990, 2022. https://doi.org/10.1093/imrn/rnaa365.
- 16. Combination theorems in groups, geometry and dynamics (joint work with Mahan Mj), In *In the tradition of Thurston II* (edited by K. Ohshika and A. Papadopoulos), Springer, 2022. https://doi.org/10.1007/978-3-030-97560-9_10.
- 17. On deformation space analogies between Kleinian reflection groups and antiholomorphic rational maps (joint work with Russell Lodge and Yusheng Luo), *Geometric and Functional Analysis*, 32:1428–1485, 2022. https://doi.org/10.1007/s00039-022-00621-8.
- 18. On dynamical gaskets generated by rational maps, Kleinian groups, and Schwarz reflections (joint work with Russell Lodge, Mikhail Lyubich, and Sergei Merenkov), *Conformal Geometry and Dynamics of the AMS*, 27:1–54, 2023. https://doi.org/10.1090/ecgd/379.
- 19. Combining rational maps and Kleinian groups via orbit equivalence (joint work with Mahan Mj), *Proceedings of the London Mathematical Society*, 126:1740–1809, 2023. https://doi.org/10.1112/plms.12517.
- 20. The Sullivan dictionary and Bowen-Series maps (joint work with Mahan Mj), EMS Surveys in Mathematical Sciences, 10:179–221, 2023. https://doi.org/10.4171/EMSS/70.
- 21. Dynamics of Schwarz reflections: the mating phenomena (joint work with Seung-Yeop Lee, Mikhail Lyubich, and Nikolai Makarov), Annales Scientifiques de l'École Normale Supérieure (Quatrième Série), 56:1825–1881, 2023. https://doi.org/10.24033/asens.2568.
- 22. Schwarz reflections and the Tricorn (joint work with Seung-Yeop Lee, Mikhail Lyubich, and Nikolai Makarov), to appear in *Annales de l'Institut Fourier*. https://arxiv.org/abs/1812.01573.

- 23. David extension of circle homeomorphisms, welding, mating, and removability (joint work with Mikhail Lyubich, Sergei Merenkov, and Dimitrios Ntalampekos), to appear in *Memoirs of the American Mathematical Society*.
 - https://arxiv.org/abs/2010.11256.
- 24. Antiholomorphic correspondences and mating I: realization theorems (joint work with Mikhail Lyubich and Jacob Mazor).

 https://arxiv.org/abs/2303.02459.
- 25. Matings, holomorphic correspondences, and a Bers slice (joint work with Mahan Mj). https://arxiv.org/abs/2304.12699.
- Mirrors of conformal dynamics: Interplay between anti-rational maps, reflection groups, Schwarz reflections, and correspondences (joint work with Mikhail Lyubich). http://arxiv.org/abs/2310.03316.
- 27. A general dynamical theory of Schwarz reflections, B-involutions, and algebraic correspondences (joint work with Yusheng Luo and Mikhail Lyubich), in preparation.
- 28. Mating parabolic rational maps with Hecke groups (joint work with Shaun Bullett, Luna Lomonaco, and Mikhail Lyubich), in preparation.

Awards/Fellowships:

- 1. Fellowship for M.Math. at Indian Statistical Institute, Bangalore, India, 2007 (declined the offer).
- 2. Fellowship for Integrated Ph.D. in Applicable Mathematics at Tata Institute of Fundamental Research, Bangalore, India, 2007 (declined the offer).
- 3. Fellowship for Ph.D. in Mathematics at Tata Institute of Fundamental Research, Mumbai, India, 2009 (declined the offer).
- 4. Fellowship for Ph.D. in Mathematics at Institute of Mathematical Sciences, Chennai, India, 2009 (declined the offer).
- 5. Fellowship for Ph.D. in Mathematics from National Board of Higher Mathematics, India, 2009.
- 6. 'Bourses d'excellence' for Research Masters in Mathematics from Université Paris 13, France, 2010.
- 7. Full scholarship for Ph.D. in Mathematics at University of Toronto, Canada, 2012 (declined the offer).
- 8. Full scholarship (Overseas Research Scholarship) for Ph.D. in Mathematics at University of Surrey, England, 2012 (declined the offer).
- 9. Fellowship for Ph.D. in Mathematics from German Research Council DFG (Grant name: Antiholomorphic Dynamical Systems and Real Slices, PI: Dierk Schleicher), Germany, 2013.
- 10. Start-up grant from Science and Engineering Research Board, India, 2020-22.
- 11. MATRICS grant from Science and Engineering Research Board, India, 2023-26.

Seminar/Conference Talks:

- 1. 'Thermodynamic formalism and Hausdorff dimension of some Julia sets I', Jacobs University, Bremen, Germany, September 2012.
- 2. 'Thermodynamic formalism and Hausdorff dimension of some Julia sets II', Jacobs University, Bremen, Germany, September 2012.
- 3. Poster presentation on 'Combinatorics and topology of the multicorns', International Centre for Mathematical Sciences, Edinburgh, UK, May 2013.
- 4. 'Combinatorics and topology of the multicorns', Universitat de Barcelona, Spain, June 2013.
- 5. 'Antiholomorphic dynamics and the multicorns', Ramakrishna Mission Vivekananda University, Calcutta, India, August 2013.
- 'Antiholomorphic dynamics and parameter spaces of polynomials', Centro di Ricerca Matematica Ennio De Giorgi, Pisa, Italy, October 2013.
- 7. 'Non-landing parameter rays of the multicorns', Jacobs University, Bremen, Germany, March 2014.
- 8. 'Non-landing parameter rays of the Tricorn', Universität Bremen, Germany, April 2014.
- 9. 'On the topological differences between the Mandelbrot set and the Tricorn', Higher School of Economics, Moscow, Russia, May 2014.
- 10. 'On the topological differences between the Mandelbrot set and the Tricorn', Banach Center Conferences, Bedlewo, Poland, July 2014.
- 11. 'On the topological differences between the Mandelbrot set and the Tricorn', Sominestationen, Holbaek, Denmark, September 2014.
- 12. 'Hausdorff dimension of Julia sets on boundaries of hyperbolic components', Jacobs University, Bremen, Germany, September 2014.
- 13. 'The topological differences between the Mandelbrot set and the Tricorn', The University of Warwick, Coventry, UK, November 2014.
- 14. 'The topological differences between the Mandelbrot set and the Tricorn', The Open University, UK, November 2014.
- 15. 'Discontinuity of the straightening map in antiholomorphic dynamics', Ramakrishna Mission Vivekananda University, Calcutta, India, January 2015.
- 16. 'Discontinuity of the straightening map in antiholomorphic dynamics', Banff International Research Station, Banff, Canada, April 2015.
- 17. 'Local-global principles for polynomial parabolic germs', Jacobs University, Bremen, Germany, April 2015.
- 18. 'Non-landing parameter rays of the Tricorn', Stony Brook University, USA, April 2015.
- 19. 'Antiholomorphic dynamics: umbilical cord wiggling, and discontinuity of the straightening map', Stony Brook University, USA, September 2015.
- 20. 'Antiholomorphic dynamics: discontinuity of the straightening map', Academy of Mathematics and Systems Science, Chinese Academy of Sciences, Beijing, China, October 2015.

- 21. 'Connectedness loci of complex polynomials: beyond the Mandelbrot set', Tata Institute of Fundamental Research, Mumbai, India, June 2016.
- 22. 'Discontinuity of straightening in antiholomorphic dynamics', University of Michigan, Ann Arbor, USA, November 2016.
- 23. 'Connectedness loci of complex polynomials: beyond the Mandelbrot set', Indian Institute of Science Education and Research, Kolkata, India, January 2017.
- 24. 'Dynamics of Schwarz reflections: mating polynomials with groups', Stony Brook University, USA, December 2017.
- 25. 'Holomorphic dynamics and Newton's method', Presidency University, Calcutta, India, January 2018.
- 26. 'Dynamics of Schwarz reflections: mating polynomials with groups', Banach Center Conferences, Będlewo, Poland, March 2018.
- 27. 'Dynamics of Schwarz reflections: mating polynomials with groups', The University of Rhode Island, USA, April 2018.
- 28. 'Dynamics of Schwarz reflections: mating polynomials with groups', Cornell University, USA, April 2018.
- 29. 'Dynamics of Schwarz reflections: mating polynomials with groups', Northwestern University, USA, May 2018.
- 30. 'Dynamics of Schwarz reflections: mating polynomials with groups', Tata Institute of Fundamental Research, Mumbai, India, June 2018.
- 31. 'Dynamics of Schwarz reflections: mating polynomials with groups', University of Toronto, Canada, October 2018.
- 32. 'Dynamics of Schwarz reflections: mating rational maps with groups', The University of Alabama at Birmingham, USA, March 2019.
- 33. 'Dynamics of Schwarz reflections: mating rational maps with groups', Universitat de Barcelona, Spain, March 2019.
- 34. 'Schwarz reflections and anti-holomorphic correspondences', Stony Brook University, USA, May 2019.
- 35. 'Dynamics of Schwarz reflections: mating rational maps with groups', The Fields Institute, Toronto, Canada, May 2019.
- 36. 'A new link between rational dynamics and Kleinian groups', Indian Institute of Technology, Gandhinagar, India, November 2019.
- 37. 'Univalent polynomials, and zeroes of harmonic polynomials', Calcutta Mathematical Society, Calcutta, India, December 2019.
- 38. 'A new link between rational dynamics and Kleinian groups', Pontificia Universidad Católica de Chile, Santiago, Chile, January 2020.
- 39. 'A new link between rational dynamics and Kleinian groups', Stony Brook University, USA, March 2020.

- 40. 'A new link between rational dynamics and Kleinian groups', Tata Institute of Fundamental Research, Mumbai, India, May 2020.
- 41. 'Reflection groups, anti-rational maps, and univalent functions', Quasiworld Online Seminar (UCLA), July 2020.
- 42. 'The Fatou-Sullivan dictionary between Kleinian groups and rational maps', Virtual Math Fest, July 2020.
- 43. 'Fatou-Sullivan dictionary, matings, and Schwarz reflections', Colloquium, Stony Brook University, USA, September 2020.
- 44. 'Matings, correspondences, and Schwarz reflections', Dynamics and Renormalization Seminar, Stony Brook University, USA, September 2020.
- 45. 'Dynamics on the Riemann sphere', Berchmans Webinar Series, St. Berchmans College, Kerala, India, November 2020.
- 46. 'Combining rational maps and Kleinian groups via orbit equivalence', IISc Geometry and Topology seminar, April 2021.
- 47. 'Schwarz reflections, Shabat polynomials, and anti-holomorphic correspondences', Stony Brook University, USA, June 2021.
- 48. 'Conformal welding and combination theorems in conformal dynamics', Pre-conference Symposium, 36th Annual Ramanujan Mathematical Society Conference, India, August 2021.
- 49. 'Interbreeding in conformal dynamics, and its applications near and far', CIRM, Luminy, France, September 2021.
- 50. 'Deformation space analogies between Kleinian reflection groups and rational maps', Tata Institute of Fundamental Research, Mumbai, India, February 2022.
- 51. 'Combining rational maps and Kleinian groups via orbit equivalence', Indo-Japan workshop on surface groups and geometric structures, April 2022.
- 52. 'Deformation space analogies between Kleinian reflection groups and rational maps', MSRI, USA, May 2022.
- 53. 'Sullivan's no wandering domain theorem', 2022 Abel Prize Colloquium: Works of Dennis Sullivan, Tata Institute of Fundamental Research, Mumbai, India, May 2022.
- 54. 'Dynamics of algebraic correspondences and mating phenomena', University of Rochester, USA, June 2022.
- 55. 'David homeomorphisms in analysis and dynamics', Banach Center Conferences, Będlewo, Poland, August 2022.
- 56. 'Dynamics of algebraic correspondences and mating phenomena', IMPA, Brazil, November 2022.
- 57. 'Deformation space analogies between Kleinian reflection groups and rational maps', 37th Annual Ramanujan Mathematical Society Conference, Chennai, India, December 2022.
- 58. 'Combining rational maps and Kleinian groups via orbit equivalence', IIT Palakkad Mathematics Department Symposium, India, February 2023.

- 59. 'Conformal welding and combination theorems in holomorphic dynamics', Recent advances in Mathematics and its applications, University of Calcutta, India, March 2023.
- 60. 'Deformation space analogies between Kleinian reflection groups and rational maps', Chennai Mathematical Institute, India, April 2023.
- 61. 'Matings, holomorphic correspondences, and a Bers slice', Kyoto Dynamical Systems Seminar, Kyoto University, Japan, June 2023.
- 62. 'Matings, holomorphic correspondences, and a Bers slice', Conformal Dynamics and Groups Seminar, Peking University, China, June 2023.
- 63. 'Matings, holomorphic correspondences, and a Bers slice', 38th Annual Ramanujan Mathematical Society Conference, Guwahati, India, December 2023.
- 64. 'Combining rational maps and Kleinian groups as algebraic correspondences', Dynamics Seminar, University of Toronto, Canada, March 2024.
- 65. 'Combining rational maps and Kleinian groups as algebraic correspondences', Colloquium, TIFR-CAM, Bangalore, India, May 2024.
- 66. 'Sullivan's dictionary, and combination theorems in conformal dynamics', Runaway seminar, TIFR-CAM, Bangalore, India, May 2024.

Mini-courses:

- 'Quasiconformal maps in holomorphic dynamics', Kerala School of Mathematics, Kozhikode, India, February 2020.
- 'Holomorphic dynamical systems', Indian Institute of Science Education and Research, Kolkata, India, November 2020.
- 3. 'Analysis and geometry on the complex plane', Vigyan Vidushi program, Tata Institute of Fundamental Research, Mumbai, India, July 2021.
- 4. 'Schwarz reflection maps and families of correspondences on the Riemann sphere', University of Rochester, USA, June 2022.
- 5. 'Introduction to complex analysis', Vigyan Vidushi program, Tata Institute of Fundamental Research, Mumbai, India, July 2022.
- 6. 'A tour of the Mandelbrot set', DMS Lecture Series, Indian Institute of Science Education and Research, Kolkata, India, September 2022.
- 'Complex dynamics a la Fatou, Julia, Brolin, and Sullivan', Kerala School of Mathematics, Kozhikode, India, May 2023.
- 8. 'Fractals arising from antiholomorphic maps and reflection groups', Advanced Studies Institute in Analysis on Fractal Spaces & Dynamical Systems, Urgench State University, Uzbekistan, August, 2023.

Teaching:

1. Teaching assistant, 'Modern Mathematics - International Summer School for Students, 2013', Jacobs University Bremen.

- 2. Teaching assistant for the course 'ODE and dynamical systems' (instructor: Dierk Schleicher), Fall semester 2013, Jacobs University Bremen.
- 3. Teaching assistant for the course 'Introductory complex analysis' (instructor: Dierk Schleicher), Fall semester 2014, Jacobs University Bremen.
- 4. Teaching assistant for the course 'Topics in complex analysis- holomorphic dynamics and Kleinian groups' (instructor: Dierk Schleicher), Spring semester 2015, Jacobs University Bremen.
- 5. MAT 127: Calculus C (course instructor), Fall semester 2015, Stony Brook University, USA.
- 6. MAT 555: Introduction to dynamical systems (course instructor), Spring semester 2016, Stony Brook University, USA.
- 7. MAT 132: Calculus II (course instructor), Fall semester 2016, Stony Brook University, USA.
- 8. MAT 308: Differential Equations with Linear Algebra (course coordinator and instructor), Spring semester 2017, Stony Brook University, USA.
- 9. MAT 125: Calculus A (course instructor), Fall semester 2017, Stony Brook University, USA.
- 10. MAT 211: Introduction to linear algebra (course instructor), Spring semester 2018, Stony Brook University, USA.
- 11. MAT 127: Calculus C (course coordinator and instructor), Fall semester 2018, Stony Brook University, USA.
- 12. MAT 310: Linear algebra (course instructor), Spring semester 2019, Stony Brook University, USA.
- 13. Dynamical systems (graduate course), Fall semester 2020, Tata Institute of Fundamental Research, Mumbai, India.
- 14. Complex analysis (graduate course), Spring semester 2022, Tata Institute of Fundamental Research, Mumbai, India.

Organization/Outreach Activities:

- 1. Member of the local organizing committee of 'Modern Mathematics International Summer School for Students', Jacobs University Bremen, July 2013.
- 2. Member of the local organizing committee and jury of '6th International Tournament of Young Mathematicians', Jacobs University Bremen, July 2014.
- 3. Member of the local organizing committee of 'Modern Mathematics International Summer School for Students', Jacobs University Bremen, July 2015.
- 4. Member of the local organizing committee of 'Modern Mathematics International Summer School for Students', Jacobs University Bremen, July 2017.
- 5. Organizer of the weekly dynamics seminar at Stony Brook University, Spring 2017-Spring 2019.
- 6. Instructor at Mathematics summer camp, Stony Brook University, July 2017.
- 7. Workshop co-instructor (with Mikhail Lyubich) at Sigma Camp, Connecticut, August 2017.

- 8. Instructor at Mathematics summer camp, Stony Brook University, July 2018.
- 9. Instructor at Sigma Camp, Connecticut, August 2018.
- 10. Coordinator of Visiting Students' Research Program, TIFR Mumbai, May-June 2020.
- 11. Mathematics colloquium organizer at TIFR Mumbai, Spring 2022-.
- 12. Organizer of one day online conference COGENT (Current Outlook on Geometry, Ergodic Theory and Number Theory), TIFR Mumbai, March 2022.
- 13. Math club talk on 'Sullivan's no wandering domain theorem', MathematiX Maths club, NISER, India, April 2022.
- 14. Organizer of 'TIFR International Colloquium on Randomness, Geometry and Dynamics', IISER Pune, India, January 2024.